

Alain F. Zuur and Elena N. Ieno

***The World of Zero-Inflated
Models. Volume 3: Using
GLLVM***

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For my two 7-year-olds, who turned my life into a 24/7 adventure, and my wife, the co-captain of this wild ride.

- Alain F. Zuur -

I dedicate this book to you dad! Thank you for everything you did for me. I will miss you a lot.

- Elena N. Ieno -

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Data sets and R code used in this book

All datasets featured in this book are available for download at <http://highstat.com>. Simply click on the Books menu and select the relevant book. You can also download all the R code from the same website. To open the ZIP files containing the R code, use the password: **<See the book>**.

Cover art

The cover drawing is by Jon Thompson (www.yellowbirdgallery.org). Mr Thompson was born in 1939 to Irish parents and has lived most of his life in Scotland. In the 1980s, he was drawn to the Orkney Islands. He is continually inspired by the landscape and bird life of Orkney. He has been creating bird art for 30 years in a variety of media, including drawing, painting, sculpture, and jewellery, never attempting to reproduce nature, but to draw parallels with it. A close-up view of a bird feather is all the inspiration he needs.

Alain F. Zuur
Newburgh, Scotland

Elena N. Ieno
Allicante, Spain